

# Measuring Latent Political Ideal Points of Twitter Users from User Description Text Data

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# Agenda

## 1 Preliminaries

- Background
- Methodology
- Data

## 2 Results and Analysis

- Posterior Distribution for Parameters
- The Relationship Between Keywords
- Model Diagnostics

## 3 Validation

- Predicting Retweeting Behavior

## 4 Conclusion and Future Work

## 5 Appendix

- JAGS Implementation

# Background

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- **Example:** Bernie Sanders is more left than Dianne Feinstein because he takes on more liberal positions and votes more liberally, even though both individuals are in the Democratic Party
- **Prior research:** Barbera (2015), Simon, Jackman, Rivers (2004), Poole (2005), Bonica (2014)

# Background

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- **Project Goal:** Estimate latent political ideal points of ordinary Twitter users using Bayesian estimation techniques
- We will focus on estimating this latent political ideal point using text from the Twitter user biographies

# Methodology: Intuitive Approach

- Specifically, we focus on extracting specific political keywords that users may put in their biographies as indicators of political affiliations
- Example:** Let's say that we were interested in the words "Clinton" and "Trump." If user  $i$ 's biography is, "I love Donald Trump!", then  $y_{i,trump} = 1$  and  $y_{i,clinton} = 0$ .

# Methodology: Technical Details

- The Bayesian model we develop largely resembles a combination of models found in Barbera (2015), Simon, Jackman, and Rivers (2004), and Hoff, Raftery, and Handcock (2002)
- Its closest analogue is a Bayesian item-response theory model



# Methodology: Technical Details

- Suppose that each Twitter user is presented with a choice to mention or not mention a political keyword, which is a word that clearly demarcates a political stance or affiliation.
- Let  $y_{ij} = 1$  if user  $i$  mentions word  $j$  in their biography, and let  $y_{ij} = 0$  otherwise.

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- Let  $y_{ij} = 1$  if user  $i$  mentions word  $j$  in their biography, and let  $y_{ij} = 0$  otherwise.
- We can consider this the function of the squared Euclidean distance in the latent political dimension between user  $i$  and word  $j$ :  
 $-\gamma(\theta_i - \phi_j)^2$ , where  $\theta_i \in \mathbb{R}$  is the latent political ideal point of Twitter user  $i$  along this latent political dimension,  $\phi_j$  is the political ideal point of word  $j$  along this political dimension, and  $\gamma$  is the discrimination parameter, or how important this relationship is to estimating the political ideal point.

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- Let  $\beta_i$  be a measure of how political an individual is on Twitter. Sometimes individuals may spam political words in their autobiographies, while others may only mention a single political keyword.

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- Then, assuming conditional independence between users, our likelihood in this model is

$$p(\mathbf{y}|\theta, \phi, \beta, \gamma) = \prod_{i=1}^n \prod_{j=1}^m (\text{logit}^{-1}(\pi_{ij}))^{y_{ij}} (1 - \text{logit}^{-1}(\pi_{ij}))^{1-y_{ij}}$$

where  $\pi_{ij} = \beta_i - \gamma(\theta_i - \phi_j)^2$ . Then, the full posterior is

$$p(\theta, \phi, \beta, \gamma|\mathbf{y}) \propto p(\mathbf{y}|\theta, \phi, \beta, \gamma)p(\theta, \phi, \beta, \gamma)$$

# Methodology: Technical Details

- We assume the following priors:  $\beta_i \sim N(\mu_\beta, \sigma_\beta^2)$ ,  $\theta_i \sim N(\mu_\theta, \sigma_\theta^2)$ , and  $\phi_j \sim N(\mu_\phi, \sigma_\phi^2)$ .
- Then, the full joint posterior distribution is

$$p(\theta, \phi, \beta, \gamma | y) \propto \prod_{i=1}^n \prod_{j=1}^m (\text{logit}^{-1}(\pi_{ij}))^{y_{ij}} (1 - \text{logit}^{-1}(\pi_{ij}))^{1-y_{ij}} \times \\ \times \prod_{i=1}^n N(\beta_i | \mu_\beta, \sigma_\beta^2) \prod_{i=1}^n N(\theta_i | \mu_\theta, \sigma_\theta^2) \prod_{j=1}^m N(\phi_j | \mu_\phi, \sigma_\phi^2)$$

# Methodology: Now in Plain English

- We want to estimate  $\theta_i$  for each user  $i$ . This is each user's ideal point along a latent left-right political continuum.
- Our assumption is that the closer the ideal point of user  $i$  to the ideal point of word  $j$  *along the same latent left-right political continuum*, the more likely user  $i$  will use word  $j$  in his or her autobiography.
- Everything else is just technical details.

# Why a Bayesian Approach?

- The number of parameters is very large (one  $\beta$  for each user, one  $\theta$  for each user, one  $\phi$  for each word), so a Bayesian approach turns what is typically a very difficult problem in classical estimation to a routine application of MCMC.
- It also allows us to incorporate previous knowledge through other studies of the distribution of ideal points of ordinary citizens through the priors. See Barbera (2015) and Bonica (2014).

# Data

- Our Twitter data comes from dissertation work of Patrick Wu.
- It was collected in the month before the November 8, 2016 general U.S. election.
- All users in this dataset use at least one of the 14 political keywords we selected, as detailed in the next slide.
- There are 9,190 user biographies in our dataset.
- To get matches, we stemmed all words in the user biographies and matched based on stemmed words.
- Thus, we are estimating 18,396 parameters.



# Data: Keyword Selection

We are analyzing 14 keywords from Twitter autobiographies:

Trump	Republican	MAGA	AlwaysTrump
Clinton	Democrat	StrongerTogether	ImWithHer
Donald	RealDonaldTrump	NeverTrump	
Hillary	HillaryClinton	NeverHillary	

# Posterior Distribution for Keywords ( $\phi_j$ )

The following table tells the posterior distribution for each keywords  $\phi_j$  (mean value, 0.01, 0.5, 0.99 quantiles and 95% credible interval):

Keyword	mean	0.01	95% cred. interval	median	0.99	SD
Trump	2.199	2.068	(2.085,2.318)	2.198	2.340	0.060
Clinton	-4.594	-4.832	(-4.791,-4.415)	-4.592	-4.384	0.096
Donald	4.686	4.477	(4.508,4.875)	4.683	4.914	0.096
Hillary	-3.757	-3.947	(-3.920,-3.600)	-3.756	-3.578	0.082
Republican	4.017	3.836	(3.859,4.186)	4.016	4.221	0.084
Democrat	-3.097	-3.274	(-3.246,-2.957)	-3.096	-2.933	0.073
RealDonaldTrump	5.411	5.167	(5.207, 5.628)	5.410	5.675	0.110
HillaryClinton	-4.874	-5.114	(-5.074,-4.683)	-4.872	-4.652	0.100
MAGA	3.831	3.651	(3.679,3.993)	3.829	4.021	0.080
StrongerTogether	-5.200	-5.454	(-5.414,-4.993)	-5.197	-4.961	0.108
NeverHillary	4.389	4.189	(4.216, 4.574)	4.387	4.604	0.090
NeverTrump	-4.145	-4.356	(-4.323,-3.981)	-4.143	-3.951	0.088
AlwaysTrump	6.476	6.141	(6.189,6.789)	6.473	6.857	0.151
ImWithHer	-3.166	-3.338	(-3.311,-3.030)	-3.164	-3.005	0.072

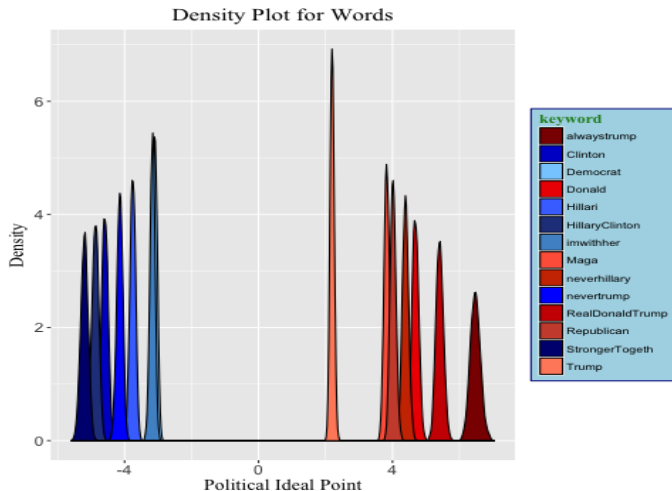
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- **AlwaysTrump** goes to the most positive side, whereas **StrongerTogether** goes to the most negative side.

# Posterior Distribution for Keywords( $\phi_j$ )



① **Left:** Democratic and **Right:** Republican party affiliated words.

# Posterior Distributions for Parameters ( $\beta_i$ , $\theta_i$ and $\gamma$ )

The following table tells the posterior distribution of individual effects ( $\beta_i$ ,  $\theta_i$ ) and discrimination parameter ( $\gamma$ ):

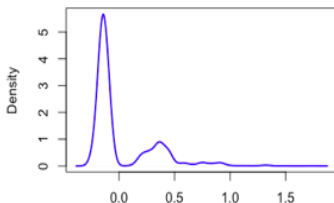
Parameter	mean	0.01	95% cred. interval	median	0.99	SD
$\beta_{avg}$	0.01	-1.80	(-1.50,1.40)	0.03	1.64	0.74
$\theta_{avg}$	0.00	-1.64	(-1.37,1.36)	0.00	1.63	0.70
$\gamma$	0.18	0.17	(0.17,0.20)	0.18	0.20	0.01

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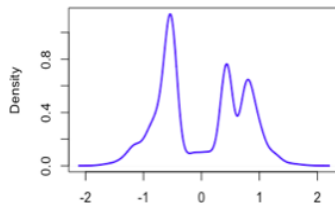
Parameter	mean	0.01	95% cred. interval	median	0.99	SD
$\beta_{avg}$	0.01	-1.80	(-1.50,1.40)	0.03	1.64	0.74
$\theta_{avg}$	0.00	-1.64	(-1.37,1.36)	0.00	1.63	0.70
$\gamma$	0.18	0.17	(0.17,0.20)	0.18	0.20	0.01

Distribution of Posterior Mean for beta



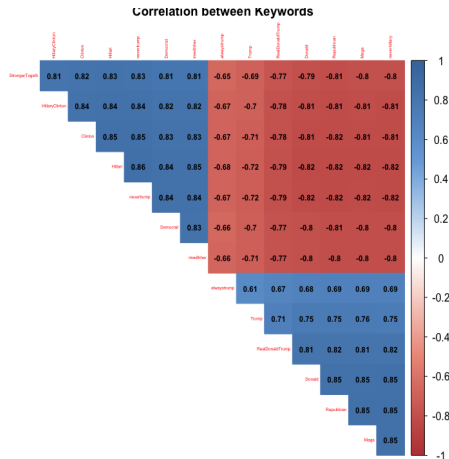
N = 9190 Bandwidth = 0.03824

Distribution of Posterior Mean for theta



N = 9190 Bandwidth = 0.1041

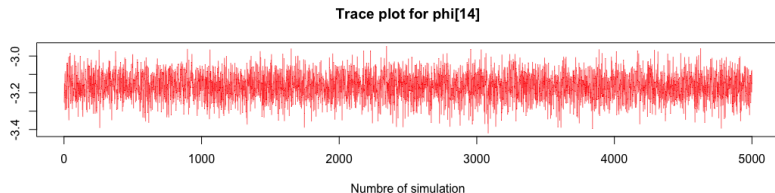
# The Relationship Between Keywords



- The correlation of  $\phi_j$  appears to be **positive/negative** if the two keywords are affiliated with the **same/opposing** party in prediction.

# Model Diagnostics

## 1 Trace plot



## 2 Geweke diagnostic test

$\phi_1$	$\phi_2$	$\phi_3$	$\phi_4$	$\phi_5$	$\phi_6$	$\phi_7$
-1.015	1.160	-1.105	0.971	-0.804	0.909	-1.054
$\phi_8$	$\phi_9$	$\phi_{10}$	$\phi_{11}$	$\phi_{12}$	$\phi_{13}$	$\phi_{14}$
1.101	-1.158	1.048	-1.148	0.929	-1.661	0.929



# Model Diagnostics

- Geweke diagnostic test statistics for 18396 parameters

1%	2.5%	25%	50%	75%	97.5%	99%
-2.318	-1.950	-0.687	-0.014	0.664	1.936	2.350

- pD: We obtained pD: 15830.61 with 18396 parameters in our model, so  $\frac{pD}{\# \text{ parameter}} < 1$ .
- Gelman-Rubin statistic: currently having trouble running on Flux...

# Validation: Predicting Retweets of Dem. and Rep. Accounts

- Although the confidence intervals on the  $\theta_i$  values are quite large, we think their width comes from our small  $n$ .
- We have the number of retweets from popular Democratic/left-leaning accounts and the total number of retweets from popular Republican/right-leaning accounts for each individual in our dataset.

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- Because many individuals do not have retweets, and because of overdispersion concerns, we use a zero-inflated negative binomial model.
- Here, the dependent variable is the number of left or right retweets, and the independent variable is the  $\theta$  values.

# Validation: Predicting Retweets of Dem. and Rep. Accounts

<b>Count</b>	<i>Dem. Accts</i>	<i>Rep. Accts</i>
(Intercept)	3.12 (0.02)	4.49 (0.02)
$\theta$	-1.22 (0.03)	1.57 (0.03)
$\log(\theta)$	-0.65 (0.02)	-1.00 (0.02)
<b>Zero-Inflated</b>		
(Intercept)	4.48 (0.17)	5.18 (0.20)
$\theta$	2.25 (0.08)	-2.03 (0.12)
$\log(1 + \text{RT Count})$	-0.91 (0.03)	-1.27 (0.04)
log likelihood	-27870	-38090

- $\log(\theta)$  denotes the overdispersion parameter.

# Validation: Predicting Other Types of Twitter Behavior

- We find that this pattern holds for retweets of Democratic members of Congress and retweets of Republican members of Congress
- We find that this pattern holds for retweets of Clinton vs. Trump
- We find that this pattern holds for the usage of hashtags typically associated with Democrats and for the usage of hashtags typically associated with Republicans
- Lastly, we find that this pattern also holds for favorites of popular Democratic accounts and favorites of popular Republican accounts.

# Conclusion and Future Work

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# Conclusion and Future Work

- This method does a good job placing words on the expected side of the political continuum.
- The ideal points estimated for each individual through  $\theta_i$  are predicting other political behaviors on Twitter.
- Extend model to people who may not use political keywords.
- Also, in the future we can implement a Metropolis-Hasting approach that fixes the word ideal points and updates ideal points for individuals only for faster computational times.



# JAGS Implementation

```
JAGS_ideal_points <- function(){  
  #Prior  
  for(j in 1:J){  
    beta[j] ~ dnorm(0,1)  
  }  
  for(k in 1:K){  
    phi[k] ~ dnorm(phi_mu,phi_tau)  
  }  
  for(j in 1:J){  
    theta[j] ~ dnorm(0,1)  
  }  
  phi_mu ~ dunif(-99999999,99999999)  
  phi_sigma ~ dunif(-99999999,99999999)  
  phi_tau <- pow(phi_sigma,-2)  
  
  gamma ~ dunif(-99999999,99999999)  
  
  #Likelihood  
  for (j in 1:J){  
    for(k in 1:K){  
      Y[j,k] ~ dbern(prob[j,k])  
      logit(prob[j,k]) <- beta[j] - gamma*pow(theta[j] - phi[k],2)  
    }  
  }  
}
```